

108. **Table of Derivatives.** In this table, u and v represent functions of x ; a , n , e represent constants ($e = 2.7183 \dots$), and all angles are measured in radians.

$$\frac{d}{dx} (x) = 1.$$

$$\frac{d}{dx} (a) = 0.$$

$$\frac{d}{dx} (u \pm v \pm \dots) = \frac{du}{dx} \pm \frac{dv}{dx} \pm \dots$$

$$\frac{d}{dx} (au) = a \frac{du}{dx}$$

$$\frac{d}{dx} (uv) = u \frac{dv}{dx} + v \frac{du}{dx}$$

$$\frac{d}{dx} \left(\frac{u}{v} \right) = \frac{v \frac{du}{dx} - u \frac{dv}{dx}}{v^2}$$

$$\frac{d}{dx} \sin u = \cos u \frac{du}{dx}$$

$$\frac{d}{dx} (u^n) = nu^{n-1} \frac{du}{dx}$$

$$\frac{d}{dx} \cos u = -\sin u \frac{du}{dx}$$

$$\frac{d}{dx} \log_a u = \frac{\log_a e}{u} \frac{du}{dx}$$

$$\frac{d}{dx} \tan u = \sec^2 u \frac{du}{dx}$$

$$\frac{d}{dx} \log_e u = \frac{1}{u} \frac{du}{dx}$$

$$\frac{d}{dx} \text{ctn } u = -\text{csc}^2 u \frac{du}{dx}$$

$$\frac{d}{dx} a^u = a^u \cdot \log_e a \cdot \frac{du}{dx}$$

$$\frac{d}{dx} \sec u = \sec u \tan u \frac{du}{dx}$$

$$\frac{d}{dx} e^u = e^u \frac{du}{dx}$$

$$\frac{d}{dx} \csc u = -\csc u \text{ctn } u \frac{du}{dx}$$

$$\frac{d}{dx} u^v = vu^{v-1} \frac{du}{dx} + u^v \log_e u \frac{dv}{dx}$$

$$\frac{d}{dx} \text{vers } u = \sin u \frac{du}{dx}$$

$$\lim_{x \rightarrow 0} \frac{\sin x}{x} = 1, \lim_{x \rightarrow 0} (1+x)^{1/x} = e = 2.71828 \dots = 1 + 1 + \frac{1}{2!} + \frac{1}{3!} + \dots$$

$$\frac{d}{dx} \sin^{-1} u = \frac{1}{\sqrt{1-u^2}} \frac{du}{dx}$$

$$-\frac{\pi}{2} \leq \sin^{-1} u \leq \frac{\pi}{2}$$

$$\frac{d}{dx} \cos^{-1} u = -\frac{1}{\sqrt{1-u^2}} \frac{du}{dx}$$

$$0 \leq \cos^{-1} u \leq \pi$$

$$\frac{d}{dx} \tan^{-1} u = \frac{1}{1+u^2} \frac{du}{dx}$$

$$\frac{d}{dx} \text{ctn}^{-1} u = -\frac{1}{1+u^2} \frac{du}{dx}$$

$$\frac{d}{dx} \sec^{-1} u = \frac{1}{u\sqrt{u^2-1}} \frac{du}{dx}, \quad -\pi \leq \sec^{-1} u < -\frac{\pi}{2}, \quad 0 \leq \sec^{-1} u < \frac{\pi}{2}$$