

MAT 136 (Calculus I), Prof. Jim Swift
Worksheet 7, on Continuity and Algebraic Limits.

1. The function $f(x) = e^{\cos(x)}$ is continuous on the set of all real numbers. Evaluate the limit.

$$\lim_{x \rightarrow 1} e^{\cos(x)} = e^{\cos(1)}$$

2. The function $f(x) = e^{-1/x^2}$ is continuous on its domain. Note that $f(0)$ is undefined. Can we conclude that $\lim_{x \rightarrow 0} f(x)$ DNE? **No.**

3. Evaluate $\lim_{x \rightarrow 2} \frac{x^2 - 3x + 2}{x - 2}$, showing all the steps and using good grammar.

$$\begin{aligned} \lim_{x \rightarrow 2} \frac{x^2 - 3x + 2}{x - 2} &= \lim_{x \rightarrow 2} \frac{(x-2)(x-1)}{(x-2)} \\ &= \lim_{x \rightarrow 2} (x-1) \quad \leftarrow \text{The magic step.} \\ &= 2-1 \\ &= \boxed{1} \end{aligned}$$

Notes $A = B = C = D = \boxed{E}$ means $A = E$, and this is the final answer

Note: ~~Don't do this!~~ $\lim_{x \rightarrow 2} \frac{x^2 - 3x + 2}{x - 2} = \frac{2^2 - 3 \cdot 2 + 2}{2 - 2} = \frac{0}{0}$
 not true = sign.

Don't write " $\lim_{x \rightarrow 2} \frac{(x-2)(x-1)}{(x-2)}$ " which is it?
 $\lim_{x \rightarrow 2} \frac{(x-2)(x-1)}{x-2}$ or $\lim_{x \rightarrow 2} (x-1)$.

Write both expressions and realize that the function is different, like in the solution above.