

examples:

Find the derivatives of these functions. (Answer with a sentence.)

1. $f(x) = \sin^3(\cos(x)) = (\sin(\cos(x)))^3$

$$f'(x) = 3(\sin(\cos(x)))^2 \frac{d}{dx} [\sin(\cos(x))] = 3\sin^2(\cos(x)) \left(\cos(\cos(x)) \frac{d}{dx} (\cos(x)) \right)$$

2. $f(x) = \sin(x^3)$

$$f'(x) = \cos(x^3) \cdot 3x^2$$

$$= 3\sin^2(\cos(x)) \cdot \cos(\cos(x)) (-\sin(x))$$
$$= -3\sin^2(\cos(x)) \cos(\cos(x)) \sin(x)$$

3. $f(x) = \exp\left(\frac{x}{1+x^2}\right)$, $f'(x) = e^{\frac{x}{1+x^2}} \frac{d}{dx} \left[\frac{x}{1+x^2} \right] = e^{\frac{x}{1+x^2}} \cdot \frac{1(1+x^2) - x(2x)}{(1+x^2)^2} = e^{\frac{x}{1+x^2}} \frac{1-x^2}{(1+x^2)^2}$