

# MAT 137 (Calculus II) Prof. Swift

## Parametric Curves in the Plane, Part 2

1. Eliminate the parameter to get an equation in terms of  $x$  and  $y$  for the parabola with parametric description  $x = 1 + t^2$ ,  $y = 3 + t$ . Write your answer in the form  $x = Ay^2 + By + C$ .
2. Eliminate the parameter to get an equation in terms of  $x$  and  $y$  for the ellipse with parametric description  $x = 3 \cos(t)$ ,  $y = 2 \sin(t)$ . Hint:  $\sin^2(t) + \cos^2(t) = 1$  for all  $t$ .
3. The parametric equations  $x = \sin(t) + \cos(t)$ ,  $y = \sin(t)$ ,  $0 \leq t \leq 2\pi$  trace out an ellipse. Find the points on this ellipse where the tangent line is horizontal. (Hint: The vertical velocity is zero when the curve has a horizontal tangent, so start by solving  $\frac{dy}{dt} = 0$  for  $t$ .)