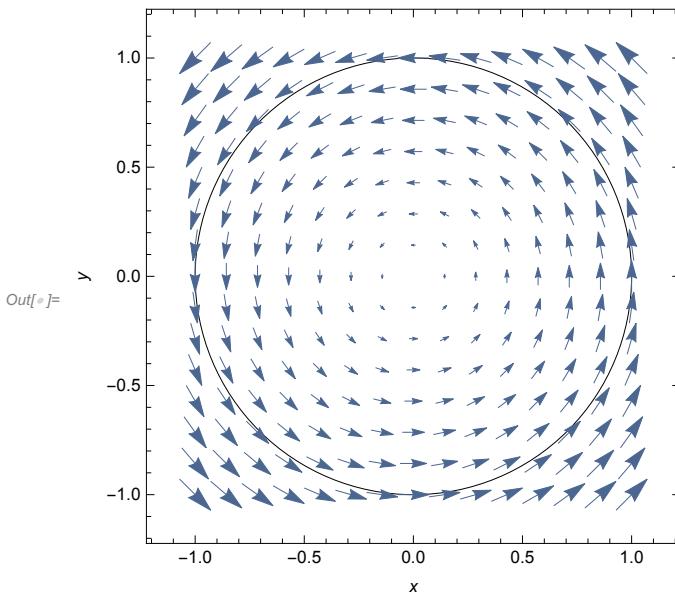


For each of these linear vector fields, the divergence of \mathbf{F} and the curl of \mathbf{F} are constant functions. The curl of \mathbf{F} is a constant times \mathbf{k} -hat, so $\text{curl}_z \mathbf{F}$ is that constant.

The flux of \mathbf{F} out through the circle is the divergence of \mathbf{F} times the area of the disk, and the circulation of \mathbf{F} around the circle is $\text{curl}_z \mathbf{F}$ times the area of the disk.

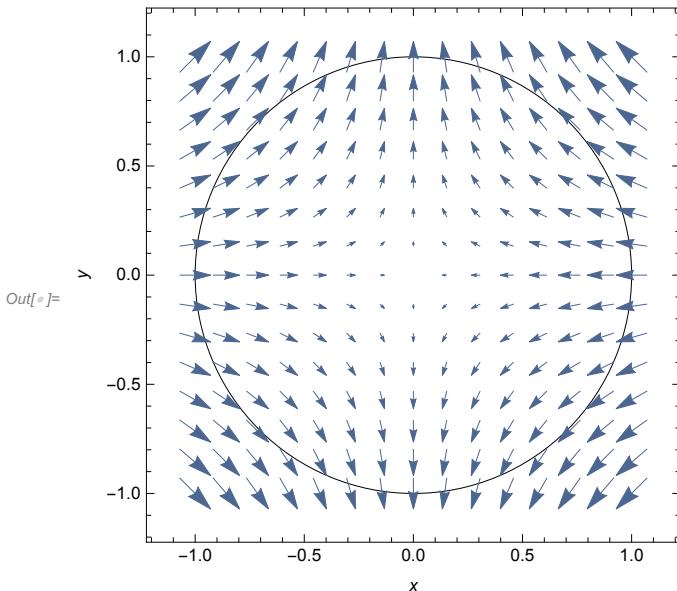
$$\mathbf{F}(x, y) = \{-y, x\}$$

$$\text{div } \mathbf{F} = 0, \text{curl}_z \mathbf{F} = 2$$



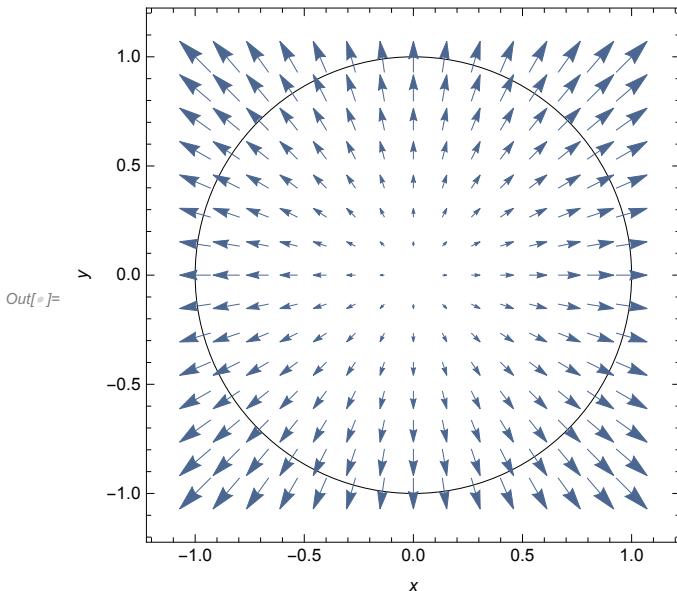
$$\mathbf{F}(x, y) = \{-x, y\}$$

$$\operatorname{div} \mathbf{F} = 0, \operatorname{curl}_z \mathbf{F} = 0$$



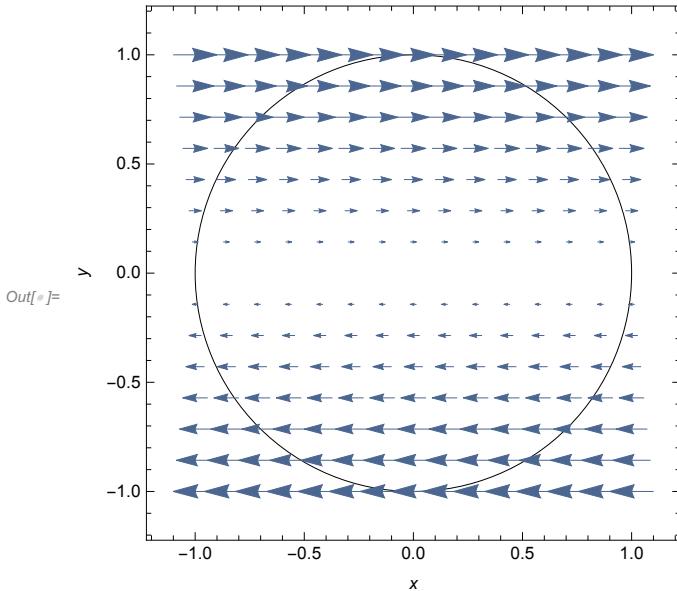
$$\mathbf{F}(x, y) = \{x, y\}$$

$$\operatorname{div} \mathbf{F} = 2, \operatorname{curl}_z \mathbf{F} = 0$$



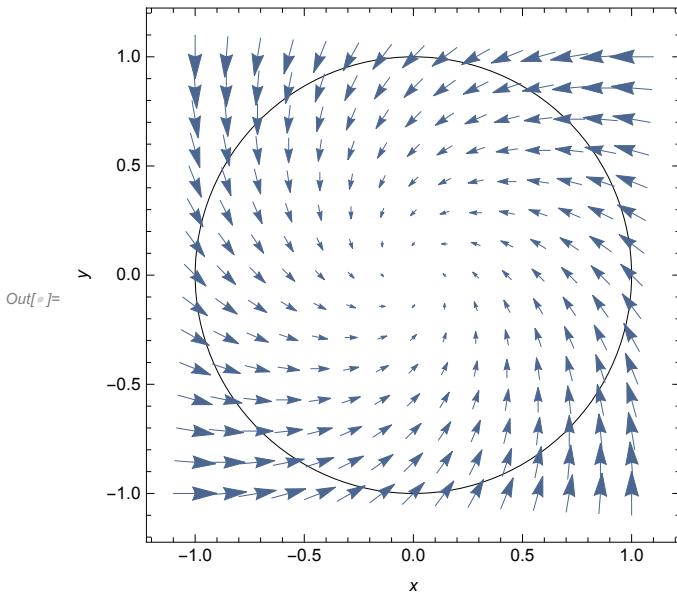
$$\mathbf{F}(x, y) = \{y, 0\}$$

$$\operatorname{div} \mathbf{F} = 0, \operatorname{curl}_z \mathbf{F} = -1$$



$$\mathbf{F}(x, y) = \{-x - y, x - y\}$$

$$\operatorname{div} \mathbf{F} = -2, \operatorname{curl}_z \mathbf{F} = 2$$



$$\mathbf{F}(x, y) = \{2, 1\}$$

$$\operatorname{div} \mathbf{F} = 0, \operatorname{curl}_z \mathbf{F} = 0$$

