

**MAT 239 (Differential Equations), Prof. Swift**  
**Worksheet 17, on Repeated and Complex Roots of the Char. Eqn.**

1. Find the general solution of the ODE  $y'' - 6y' + 9y = 0$  for  $y(t)$ .
  
2. Find the general solution of the ODE  $y'' + 2y' + 5y = 0$  for  $y(t)$ .
  
3. Suppose one solution to a 2nd order linear homogeneous ODE with constant coefficients (LHODECC) is  $y(t) = 5e^{2t} \cos(3t)$ .
  - (a) What is the general solution of the ODE? (Frank Sinatra: "You can't have one with the other.")
  - (b) What are the roots of the characteristic equation?
  - (c) What is the ODE?