# MAT 239 (Differential Equations), Prof. Swift Worksheet 24, Test Review 

1. Write down the general solution to $(D-2)^{3}(D-4) y=0$. The independent variable is $x$.
2. Write down the form of a particular solution to $(D-2)^{3}(D-4) y=5 e^{2 x}+7 \sin (4 x)$
3. Suppose that
$y_{1}(t)$ solves the IVP $y^{\prime \prime}+e^{t} y^{\prime}+\sin (t) y=0, y(0)=1, y^{\prime}(0)=0$,
$y_{2}(t)$ solves the IVP $y^{\prime \prime}+e^{t} y^{\prime}+\sin (t) y=0, y(0)=0, y^{\prime}(0)=1$, and
$y_{3}(t)$ solves the IVP $y^{\prime \prime}+e^{t} y^{\prime}+\sin (t) y=t^{2}, y(0)=0, y^{\prime}(0)=0$.

Write down the solution to the IVP $y^{\prime \prime}+e^{t} y^{\prime}+\sin (t) y=t^{2}, y(0)=\alpha, y^{\prime}(0)=\beta$ as a linear combination of $y_{1}, y_{2}$, and $y_{3}$.

