## MAT 239 (Differential Equations), Prof. Swift Worksheet 24, Test Review

1. Write down the general solution to  $(D-2)^3(D-4)y = 0$ . The independent variable is x.

2. Write down the form of a particular solution to  $(D-2)^3(D-4)y = 5e^{2x} + 7\sin(4x)$ 

3. Suppose that

 $y_1(t)$  solves the IVP  $y'' + e^t y' + \sin(t)y = 0, y(0) = 1, y'(0) = 0,$ 

 $y_2(t)$  solves the IVP  $y'' + e^t y' + \sin(t)y = 0$ , y(0) = 0, y'(0) = 1, and

 $y_3(t)$  solves the IVP  $y'' + e^t y' + \sin(t)y = t^2$ , y(0) = 0, y'(0) = 0.

Write down the solution to the IVP  $y'' + e^t y' + \sin(t)y = t^2$ ,  $y(0) = \alpha$ ,  $y'(0) = \beta$  as a linear combination of  $y_1, y_2$ , and  $y_3$ .