MAT 239 (Differential Equations) Prof. Swift Worksheet 5. First Order ODEs, Inspection and Separation of Variables

1. Find the general solution to $\frac{dy}{dx} = 2y$, by inspection if possible.

2. Solve the initial value problem (IVP) $\frac{dy}{dx} = 2y$, y(0) = 3, by inspection if possible.

3. Find the solution to the IVP $\frac{dy}{dx} = \frac{1}{e^y}$, y(0) = 0, using separation of variables. Find the interval of existence of the solution.