

## Bézier Curve

To construct the cubic Bézier curves  $C_0, \dots, C_{n-1}$  in parametric form, where  $C_i$  is represented by

$$(x_i(t), y_i(t)) = (a_0^{(i)} + a_1^{(i)}t + a_2^{(i)}t^2 + a_3^{(i)}t^3, b_0^{(i)} + b_1^{(i)}t + b_2^{(i)}t^2 + b_3^{(i)}t^3),$$

for  $0 \leq t \leq 1$ , as determined by the left endpoint  $(x_i, y_i)$ , left guidepoint  $(x_i^+, y_i^+)$ , right endpoint  $(x_{i+1}, y_{i+1})$ , and right guidepoint  $(x_{i+1}^-, y_{i+1}^-)$  for each  $i = 0, 1, \dots, n-1$ :

INPUT  $n; (x_0, y_0), \dots, (x_n, y_n); (x_0^+, y_0^+), \dots, (x_{n-1}^+, y_{n-1}^+); (x_1^-, y_1^-), \dots, (x_n^-, y_n^-)$ .

OUTPUT coefficients  $\{a_0^{(i)}, a_1^{(i)}, a_2^{(i)}, a_3^{(i)}, b_0^{(i)}, b_1^{(i)}, b_2^{(i)}, b_3^{(i)}, \text{ for } 0 \leq i \leq n-1\}$ .

*Step 1* For each  $i = 0, 1, \dots, n-1$  do Steps 2 and 3.

*Step 2* Set  $a_0^{(i)} = x_i$ ;

$$b_0^{(i)} = y_i;$$

$$a_1^{(i)} = 3(x_i^+ - x_i);$$

$$b_1^{(i)} = 3(y_i^+ - y_i);$$

$$a_2^{(i)} = 3(x_i + x_{i+1}^- - 2x_i^+);$$

$$b_2^{(i)} = 3(y_i + y_{i+1}^- - 2y_i^+);$$

$$a_3^{(i)} = x_{i+1} - x_i + 3x_i^+ - 3x_{i+1}^-;$$

$$b_3^{(i)} = y_{i+1} - y_i + 3y_i^+ - 3y_{i+1}^-;$$

*Step 3* OUTPUT  $(a_0^{(i)}, a_1^{(i)}, a_2^{(i)}, a_3^{(i)}, b_0^{(i)}, b_1^{(i)}, b_2^{(i)}, b_3^{(i)})$ .

*Step 4* STOP. ■